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Boundary-Control Vector (BCV) Motion Field Representation and Estimation By Using A Markov Random Field Model

by

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Boundary-Control Vector (BCV) Motion Field Representation and Estimation By Using A Markov Random Field Model *

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Abstract

A new motion field representation based on the boundary-control vector (BCV) scheme for video coding is examined in this work. With this scheme, the motion field is characterized by a set of control vectors, which are motion vectors associated with the center points of blocks, and a set of boundary functions, which specify the continuity of the motion field across adjacent blocks. For BCV-based motion field estimation, an optimization framework based on the Markov random field model and a maximum a posterior (MAP) criterion is used. The new scheme effectively represents complex motions such as translation, rotation, zooming and deformation and does not require complex scene analysis. Compared with MPEG of similar decoded SNR (signal-to-noise ratio) quality, 15-35% bit rate saving can be achieved in the proposed scheme with a more pleasant visual quality.

Keywords: motion estimation, motion representation, video coding, boundary-control vector (BCV), Markov random field.

1 Introduction

In image sequence coding, image frames are often encoded by two parts, i.e. the motion field which represents the change in the sequence and the displacement frame difference (DFD) which represents the residual error after motion compensation. Since both the motion field and DFD have to be transmitted to the receiver, a well designed video coder should balance the bits used in these two parts. Other factors of consideration in video coder design include computational cost, hardware complexity and the domain of applicability.

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We can roughly classify existing motion field representations into block-based, pel-based and model-based three categories. The block-based representation has been widely used and adopted by several standards such as H.261 [16] and MPEG [6]. It divides an image frame into nonoverlapping blocks, and represents the motion field in each block with a translation vector. This representation is generally applicable and concise. A differential coding can be used to further reduce the redundancy between motion vectors by exploiting their spatial correlation. The block-based motion field can be estimated by using a straightforward block matching algorithm (BMA) or its variants. However, the block-based scheme has some limitations. It does not well represent complicated motion types such as rotation, zooming and deformation, neither the motion boundaries of moving objects. The block effect caused by motion discontinuity between two adjacent blocks is subjectively annoying. To obtain a better decoded image quality, we have to use more bits to represent the DFD so that the total bit rate increases. Research has been performed to overcome the above shortcomings. Orchard [17] incorporated motion discontinuity into the block-based motion representation to obtain substantial quality improvement along moving object boundaries. The discontinuity between the motion vectors in adjacent blocks however still exists. Bergeron [1], Fuh [4], Papadopoulos [18] and Seferidis [20], [21] used more complex functions such as affine, perspective, bilinear, 2nd-order polynomial transformations to represent the motion field inside each block which require more bits in the coding of motion field.

For the pel-based representation, each pixel has its own motion vector. An arbitrary motion field can be easily represented by this scheme. The tradeoff is that it requires a lot of bits in representing such a dense motion field. To avoid the transmission of the bits for the dense motion field, one approach [15] is to derive the motion field of the current frame from that of the previous one in the encoder as well as the decoder. Since the decoder contains a complicated motion estimation unit, its cost and decoding time become issues. Furthermore, since not all motion in a video sequence can be well predicted and noise in the scenery can greatly influence the result of the estimation algorithm, the predicted gain is usually low. Due to these reasons, the pel-based motion estimation approach is not widely used now.

The model-based approach [2, 7, 14, 25], has received a lot of attention recently. Scenery is segmented into objects and the background by using image analysis tools in encoding. The shape, texture and motion information of objects are then transmitted. Image scenery is regenerated from the transmitted shape, texture and motion information with the computer graphic technique at the decoder. The model-based coding scheme has two major advantages, i.e. high compression efficiency and visually insensitive distortion. Since the shape and texture information of objects

are relatively steady across multiple frames, we only have to transmit a small amount of motion information so that the compression efficiency can be high. When the error occurs in estimation or representation, the distortion leads to small changes in the shape (geometrical deformation), texture and position of the object, which is less sensitive to human eyes in comparison with the block effect. The main shortcoming of the model-based scheme is that it requires complex scene analysis which is very expensive to implement. Coding scenery is usually restricted to simplify the image analysis task (e.g. the head-and-shoulder video sequence) so that the applicability of the model-based approach is greatly limited.

In this research, we develop a novel motion field representation scheme in which the motion field is characterized by boundaries and motion vectors in a predefined grid points known as the control vectors. In contrast with the block-based motion representation, the control vector does not represent the motion field for every pixel within the block but only for the control point. The motion vector at points other than control points are obtained via interpolation. The boundary function in the BCV-scheme allows the discontinuity of the motion field so that the unrealistic global smooth constraint can be removed. The new boundary-control vector (BCV) scheme can describe many different complex motions such as translation, rotation, zooming and deformation and is applicable to a wide variety of scenes with a very concise representation. Compared with the model-based scheme, the BCV-based does not require complicated scenery analysis. For more details on the BCV motion field representation and the comparison of this new scheme with other traditional representations, we refer to the discussion in Sections 2.2 and 2.3.

This paper is organized as follows. The boundary-control vector (BCV) motion field representation is introduced in Section 2. A framework is proposed to estimate the BCV motion field based on the Markov random field model. The coding of predicted error after BCV motion compensation is discussed in Section 4. Experimental results are given in Section 5 to demonstrate the performance of our proposed method. Concluding remarks are presented in Section 6.

2 Boundary-Control Vector (BCV) Motion Field Representation

2.1 Control Vectors and Boundaries

Consider an image of size $N \times N$ which can be divided into $B \times B$ nonoverlopping blocks of size $K \times K$ (i.e. $N = B \times K$). We choose the center of each block as the control point so that the

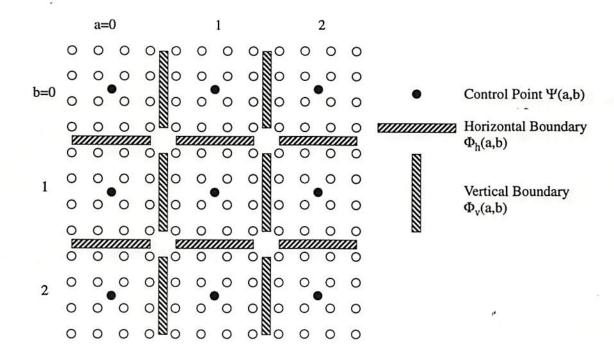


Figure 1: Illustration of control points and boundaries with K=4, where the empty circle denotes the pixel position.

position of each control point can be expressed as

$$\Psi(a,b) = (aK + \frac{K+1}{2}, bK + \frac{K+1}{2}), \quad 0 \le a, b \le B - 1, \tag{2.1}$$

where, without loss of generality, K is assumed to be an even number. These control points are fixed throughout the entire image sequence. We use Ψ to denote the set of all control points. The motion vector at control point $\Psi(a,b)$ at time t is denoted by $\mathbf{D}(a,b,t)$. It is simply called the control vector. We use \mathbf{D}_t to denote the set of all control vectors at time t. Along the lower and right boundaries of the block centered at $\Psi(a,b)$, we define, respectively, binary functions $E_h(a,b,t)$ and $E_v(a,b,t)$ whose value is 1 if there is a discontinuity in the motion field along the corresponding boundary. Otherwise, it is 0. We denote the location of the boundary as $\Phi_h(a,b)$ and $\Phi_v(a,b)$. For convenience, we say a boundary exists if its value is 1. We use the vector notation $\mathbf{E}(a,b,t)$ to denote the boundary pair $(E_h(a,b,t), E_v(a,b,t))$ and E_t is the set of all boundary functions at time t. Correspondingly, Φ is the set of all boundaries. An illustration of control points and boundaries is given in Fig. 1.

2.2 BCV Motion Field

In BCV motion field representation, the control vector $\mathbf{D}(a,b,t)$ does not represent the motion field for every pixel within the block centered at (a,b) but only for the control point $\Psi(a,b)$. The motion vector at points other than control points are obtained via interpolation. It was however observed [22] that most of the motion compensated errors occur around the boundaries of moving objects with the block-based method, since the DFD around moving object boundaries and the DFD inside the object can behave quite differently. By introducing the motion field boundary, we can locate motion discontinuity and treat the two kinds of DFD separately. The unrealistic global smooth constraint of the motion field can therefore be removed to improve the overall video coding efficiency.

The interpolation process is classified into 4 different modes, which are summarized in Fig. 2. When no boundary exists among four neighboring control points, a bilinear interpolation is applied. It is called the basic mode. When boundaries exist, some motion field discontinuity is present and the four neighboring control points can be divided into 2-2 or 3-1 pairs as shown in Fig. 2. The 2-2 pair case is called mode B, and a linear interpolation is performed at the pixel of interest by using the two control vectors associated with the region. The 3-1 pair case can be further classified into modes A1, A2 and C. In mode C, there is one only control vector associated with the region so that all pixels inside take the same constant value. The linear interpolation is performed by using the three adjacent control vectors in mode A1. Finally, for pixels belonging to mode A2, we adopt a simple linear weighting scheme. In developing the above interpolation rules, we want to keep them as simple as possible so that the motion vector of each pixel can be computed effectively and, in the mean time, take the discontinuity of the motion field into account.

An example of the interpolated motion field is shown in Fig. 3. The interpolated dense motion field is represented by

$$\mathbf{d}(x, y, t) = \operatorname{gen}\{\mathbf{D_t}, \mathbf{E_t}\},\$$

where we use gen to denote that a motion field is uniquely specified by the sets $\mathbf{D_t}$ and $\mathbf{E_t}$.

2.3 Comparison of Motion Field Representations

It is worthwhile to comment on the unique features of the proposed BCV-scheme in comparison with the three other motion field representations, i.e. pel-based, block-based and model-based representations.

With respect to the pel-based motion representation, the motion boundary of the BCV scheme

Mode	Figure	Interpolation region	Interpolation Scheme		
Basic	λ γ γ γ γ γ γ γ γ	□ABCD	$d(x, y, t) = D_A + \frac{x'}{K} (D_B - D_A) + \frac{y'}{K} (D_C - D_A) - \frac{x'y'}{K^2} (D_A + D_D - D_B - D_C) $ (B.1)		
Al	^	ДАВС	$d(x, y, t) = D_A + \frac{x'}{K} (D_B - D_A) + \frac{y'}{K} (D_C - D_A) $ (B.2)		
A2	γ 1	ΔΒΟΓυ ΔϹΟΕ	$d(x, y, t) = \frac{K - y'}{2K - x' - y'} D_B + \frac{K - x'}{2K - x' - y'} D_C$ (B.3)		
В	A	DAEFC	$d(x, y, t) = \frac{y'}{K} D_C + \frac{K - y'}{K} D_A$ (B.4)		
С	Λ Ε Β X X. (X,Y,D) F O	□AEOF	$d(x, y, t) = D_A \tag{B.5}$		

Figure 2: Summary of interpolation rules for BCV motion field representation, where A, B, C and D denote four control points, D_A , D_B , D_C and D_D are the associated control vectors, and a solid line indicates the presence of boundary discontinuity.

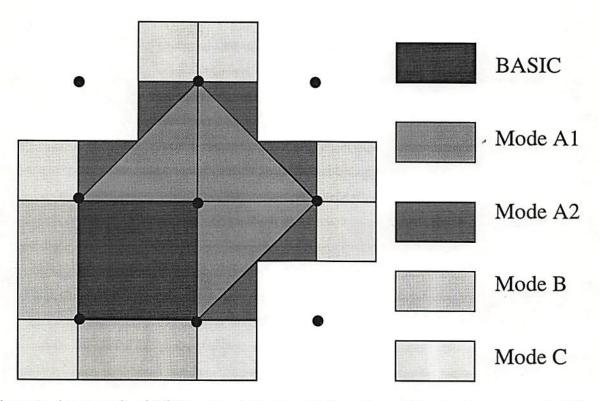
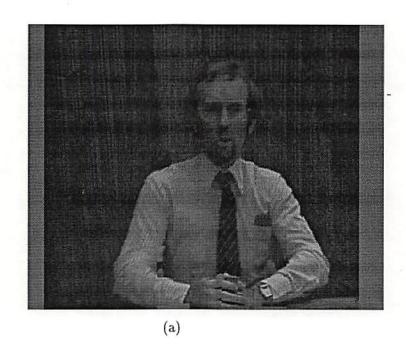


Figure 3: An example of BCV motion field interpolation where different colors represent different interpolation modes.

is relatively coarse, i.e. only represented in block accuracy. This is a tradeoff between the predicted gain that can be achieved and the bits required to transmit the boundary information. For example, with pel-accurate boundaries, we still cannot describe all interframe changes, say, the exposure region. The estimation result from the pel-based approach can be easily affected by noise, and the estimation error in the object boundary can cause degradation in the displacement frame. Although the distortion is restricted to a very small region, it is visually annoying since the characteristics of the background and the moving object are quite different. Furthermore, since the DFD contains a lot of high frequencies in the transform domain, it is usually difficult to compress. In the BCV scheme, we use the coarse-level boundaries and admit that there may exist some significant DFD around boundaries in the displacement frame. Although more bits are required to encode the DFD, the bits used to encode the motion information can be greatly saved.

The motion field in the block-based representation is constant over each block and in general not continuous along the block boundary. In contrast, the BCV-based motion field is continuous if there is no boundary between neighboring control points. The continuity of the motion field helps to remove the visually annoying block effect in the displacement frame. Although the bilinear interpolation used only provides an approximation of a complex motion field and the control vectors may have errors, the derivative object in the displacement frame only deforms slightly. Human eyes are less sensitive to these smooth errors. Along the object boundary, since only coarse boundary is used in BCV, the block effect remains and the DFD in these regions is large. The area of these regions is much smaller than that appearing in the block-based representation so that the coding efficiency of the BCV scheme is still higher. More importantly, the BCV-based motion field can represent a large class of complicated motions more accurately. The translation and rotation of objects formed by planar surfaces in the 3-D space can be well described by BCV. For the more complicated object movement, the bilinear interpolation scheme used by BCV serves as a good first order approximation of the true motion field. The BCV-based motion field can be stored or transmitted almost as efficiently as the block-based motion field. In addition to control vectors, only a small number of bits are required to encode the boundary information. To illustrate the visual difference by using the BCV and block-based methods, we show two coded displacement frames for the TREVOR image sequence in Fig. 4. Even though the displacement frames only differ by 1.77 dB in Fig. 4, the subjective quality of the BCV-based displacement frame is much better. There is a very visible block effect in the block-based method, e.g. the region of the right hand and fingers. In contrast, the BCV-based displacement frame is smoother with no visible block effect.



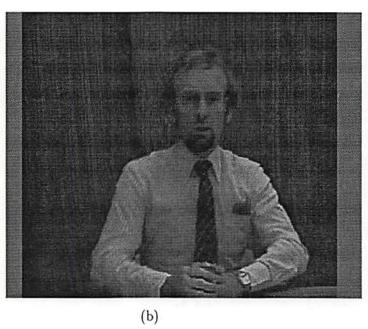


Figure 4: Comparison of displacement frames with (a) block-based scheme (0.0186bpp, 29.80dB) and (b) BCV scheme (0.0228bpp, 31.57dB).

The BCV motion field representation is quite different from the object or model-based coding scheme, in which objects in the scene have to be analyzed first. No complex image analysis is required by BCV, and no a prior knowledge about the image scenery is needed so that the BCV scheme is applicable to a wide variety of scenes. A related video coding scheme known as the active mesh [24] uses a deformable mesh structure to describe the motion field, where complex image analysis is required to track the change of the structure, say, the merge and creation of the mesh. With a set of position invariant control vectors in BCV, the motion estimation task can be greatly simplified.

3 Estimation of Control Vectors and Boundary Functions

3.1 Problem Formulation

In this section, we focus on the estimation problem for the BCV representation scheme presented in the previous section. The parameters to be estimated include the control vectors and the boundary functions. We use

$$\mathbf{f_t} = \{ f(x, y, t) \mid 0 \le x < N, \ 0 \le y < N, \ x, y \in \mathbf{I} \}$$

to denote the image of size $N \times N$ at time instance t. Let Δt be the time interval between two successive frames. Then, the estimation problem can be stated mathematically as: given $\mathbf{f_t}$ and $\mathbf{f_{t-\Delta t}}$, we want to determine the set $\mathbf{D_t}$ of control vectors and the set $\mathbf{E_t}$ of boundary functions. Once $\mathbf{D_t}$ and $\mathbf{E_t}$ are specified, the motion vector at every pixel can be uniquely determined via interpolation.

To calculate the BCV-based motion field, the following the maximum a posterior (MAP) criterion [19] is considered:

$$P(\mathbf{E}_t^*, \mathbf{D}_t^* \mid \mathbf{f}_t, \mathbf{f}_{t-\Delta t}) \equiv \max_{\mathbf{E}_t, \mathbf{D}_t} P(\mathbf{E}_t, \mathbf{D}_t \mid \mathbf{f}_t, \mathbf{f}_{t-\Delta t}).$$

By applying the Bayes rule [11], we have

$$P(\mathbf{E_t}, \mathbf{D_t} \mid \mathbf{f_t}, \mathbf{f_{t-\Delta t}}) = \frac{P(\mathbf{f_{t-\Delta t}} \mid \mathbf{E_t}, \mathbf{D_t}, \mathbf{f_t}) P(\mathbf{E_t}, \mathbf{D_t} \mid \mathbf{f_t})}{P(\mathbf{f_{t-\Delta t}} \mid \mathbf{f_t})}.$$

The denomenator term $P(\mathbf{f_{t-\Delta t}} \mid \mathbf{f_t})$ is independent of $\mathbf{E_t}$ and $\mathbf{D_t}$ and can be ingored in the optimization procedure. Thus, the above MAP problem is equivalent to the maximization of the numerator

$$P(\mathbf{f_{t-\Delta t}} \mid \mathbf{E_t}, \mathbf{D_t}, \mathbf{f_t}) P(\mathbf{E_t}, \mathbf{D_t} \mid \mathbf{f_t}). \tag{3.1}$$

The $P(\mathbf{f_{t-\Delta t}} \mid \mathbf{E_t}, \mathbf{D_t}, \mathbf{f_t})$ and $P(\mathbf{E_t}, \mathbf{D_t} \mid \mathbf{f_t})$ are related, respectively, to the displacement frame difference and *a prior* distribution of the control vector set $\mathbf{D_t}$ and the motion boundary set $\mathbf{E_t}$ as detailed below.

Let us first focus on the term $P(\mathbf{f_{t-\Delta t}} \mid \mathbf{E_t}, \mathbf{D_t}, \mathbf{f_t})$. When the motion field is generated via

$$\mathbf{d}(x, y, t) = \operatorname{gen}\{\mathbf{E_t}, \mathbf{D_t}\},$$

the displacement frame at time t is obtained by translating the image at $t - \Delta t$, i.e.

$$DF(x, y, t) = f(x - d_x(x, y, t), y - d_y(x, y, t), t - \Delta t),$$

and the difference between the frame f_t and the displacement frame is called the displacement frame difference and denoted by

$$DFD(x, y, t) = f(x, y, t) - DF(x, y, t).$$

The vector forms of the displacement frame and displacement frame difference are given by $\mathbf{DF_t}$ and $\mathbf{DFD_t}$, respectively. It is straightforward to derive that

$$P(\mathbf{f}_{t-\Delta t} \mid \mathbf{E}_{t}, \mathbf{D}_{t}, \mathbf{f}_{t}) = P(\mathbf{DF}_{t} \mid \mathbf{E}_{t}, \mathbf{D}_{t}, \mathbf{f}_{t})$$

$$= P(\mathbf{f}_{t} - \mathbf{DFD}_{t} \mid \mathbf{E}_{t}, \mathbf{D}_{t}, \mathbf{f}_{t})$$

$$= P(-\mathbf{DFD}_{t} \mid \mathbf{E}_{t}, \mathbf{D}_{t}, \mathbf{f}_{t}). \tag{3.2}$$

Empirically speaking, the displacement frame difference DFD_t is independent of E_t , D_t and f_t and can be modeled as a white Gaussian function

$$P(\mathbf{DFD_t}) = (2\pi\sigma^2)^{-\frac{N^2}{2}} \exp\left\{-\frac{1}{2\sigma^2} \sum_{(x,y)} DFD^2(x,y,t)\right\},$$
 (3.3)

where the deviation σ can be predicted via

$$\sigma = \sqrt{\frac{1}{N^2} \sum_{(x,y)} DFD^2(x,y,t-\Delta t)}.$$

Based on (3.2) and (3.3), we conclude that

$$P(\mathbf{f_{t-\Delta t}} \mid \mathbf{E_t}, \mathbf{D_t}, \mathbf{f_t}) = (2\pi\sigma^2)^{-\frac{N^2}{2}} \exp\left\{-\frac{1}{2\sigma^2} \sum_{(x,y)} DFD^2(x,y,t)\right\}.$$

The Markov random field (MRF) model can be used to determine a prior probability distribution $P(\mathbf{E_t}, \mathbf{D_t} \mid \mathbf{f_t})$, which is detailed below.

3.2 Markov Random Field Model

The Markov random field (MRF) model has been successfully used in image restoration [5], motion detection [23], and motion estimation [3, 10]. In this work, it is used for BCV-based motion field representation. In this subsection, we give a brief description of the MRF model.

Definition 1 Let $S = \{s_1, s_2, \dots, s_N\}$ be a set of sites and G(s) the set of neighbors of $s \in S$. We call $G(S) = \{G(s) \mid s \in S\}$ a neighborhood system if the following three conditions are satisfied:

- 1. $G(s) \subset S$,
- 2. $s \notin G(s)$,
- 3. $s \in G(r) \iff r \in G(s)$.

The pair $\{S, \mathcal{G}(S)\}$ is called a graph.

We assume that every control vector D(a,b,t) and boundary element E(a,b,t) only correlates with others in a small neighborhood for the BCV scheme. A first-order neighborhood system $\mathcal{G}(S)$ is illustrated in Fig. 5, which consists of two parts: the neighborhood system of control point $G(\Psi(a,b))$ and the neighborhood system of boundary $G(\Phi(a,b))$. Thus, the control vector set $\mathbf{D_t}$ and the boundary set $\mathbf{E_t}$ can be treated as a coupled MRF with joint sites \mathbf{S} :

$$S = \Psi \cup \Phi$$
.

Definition 2 A subset $C \subset S$ is a clique, if C satisfies

$$\forall r, s \in \mathbb{C}, \quad r \neq s \Longrightarrow s \in \mathbb{G}(r).$$

All cliques for the BCV scheme are depicted in Fig. 6. We use C(S) to denote the set of all cliques in S.

Definition 3 Let $X = \{x(s) \mid s \in S\}$ denote a family of random variables indexed by S, $\Omega_k = \{\omega(s_k) \mid s_k \in S\}$ the configuration space of $x(s_k)$ and $\Omega = \{\omega = (\omega(s_1), \omega(s_2), \dots, \omega(s_N))\}$ the configuration space of the random variable set X. Then, X is a markov random field (MRF) with respect to $\mathcal{G}(S)$, if

1.
$$P(X = \omega) > 0$$
 $\forall \omega \in \Omega$,

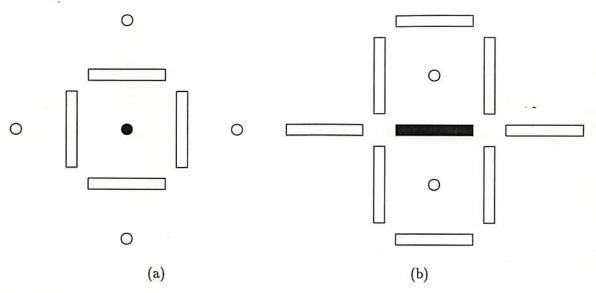


Figure 5: The neighborhood system for the BCV scheme: (a) neighborhood system $G(\Psi(a,b))$ of control point $\Psi(a,b)$ and (b) neighborhood system $G(\Phi(a,b))$ of boundary $\Phi(a,b)$.

2.
$$P(x(s) = \omega(s) \mid x(r) = \omega(r), r \neq s) = P(x(s) = \omega(s) \mid x(r) = \omega(r), r \in G(s)),$$

or the probability distribution of random variable x(s) is only relevant to its neighborhood G(s).

There is an important theorem regarding the probability distribution of the MRF.

Theorem 1 The random variable set X is a MRF with respect to G(S) if and only if

$$P(\mathbf{X} = \omega) = \frac{1}{A} \exp \left\{ -\sum_{\mathbf{C} \in C(\mathbf{S})} V_C(\omega) \right\},$$

where each $V_C(\omega)$ is a potential function depends only on those x(s) for which $s \in \mathbb{C}$, and A is a normalizing constant so that

$$\int_{\omega \in \Omega} P(X = \omega) d\omega = 1.$$

The proof of the theorem can be found in [8].

In the application of MRF, we are often required to determine the probability distribution of X. By using Theorem 1, we define the probability distribution $P(X = \omega)$ by designating the potential function $V_C(\omega)$ for each clique $C \in C(S)$ given in Fig. 6. There are 16 cliques in Fig. 1. In the following, we argue that some cliques can be eliminated or merged with others so that we can focus on the potential definition of a shorter list. Note first that the control vector D(a, b, t) primarily

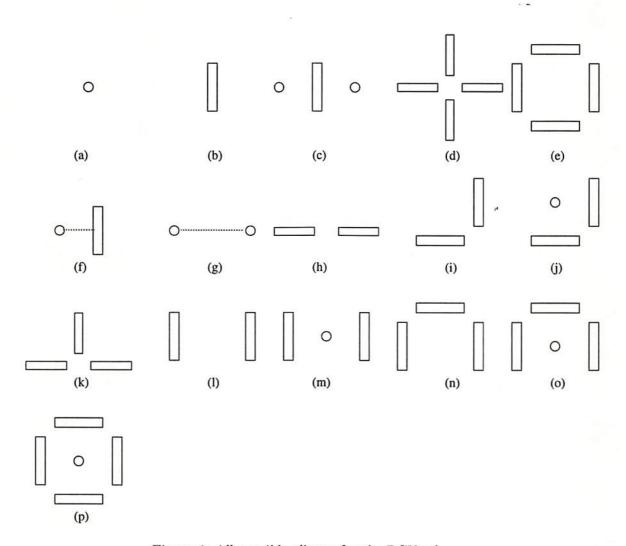


Figure 6: All possible cliques for the BCV scheme.

correlates with its neighboring control vector. It is reasonable to assume that the potential of clique (p) is just the sum of the potentials of cliques (e) and (a) so that there is no need to define the potential for (p) independently. Similarly, the potentials of cliques (f),(j),(m),(o) can be derived from those of other cliques. Second, we may optionally merge a clique to its superset due to some physical consideration. For example, clique (n) can be merged to clique (e) since they both provide the shape description for boundary elements and clique (n) is a subset of clique (e). By using the same reason, clique (l) can be merged to clique (e), cliques (h),(i),(k) can be merged to clique (d), and clique (g) can be merged to clique (c). However, although clique (b) is a subset of clique (c), they have different physical meanings. That is, clique (b) is used to relate a boundary element with the intensity edges while clique (c) relates neighboring control vectors separated by a boundary element. Thus, we decide to treat them differently.

After carefully merging and eliminating the unnecessary clique forms, we choose five cliques (a)-(e) to represent the *a prior* distribution of the motion field $P(\mathbf{E_t}, \mathbf{D_t} \mid \mathbf{f_t})$ where each one has a unique physical sense. We discuss how to define the potential for each of these cliques in the following.

C_a = {Ψ(a,b)} - the probability distribution of a single control vector D(a,b,t).
 The potential of clique (a) is determined by the a prior distribution of the single control vector D(a,b,t). By assuming that D(a,b,t) is Gaussian-distributed, the potential of clique (a) can be written as:

$$V_{C_a}(\mathbf{E_t}, \mathbf{D_t}, \mathbf{f_t}) = V_{C_a}(\mathbf{D_t}) = \alpha_a ||D(a, b, t)||^2.$$

If D(a, b, t) has the Laplacian distribution, the potential of clique (a) becomes

$$V_{C_a}(\mathbf{E_t}, \mathbf{D_t}, \mathbf{f_t}) = V_{C_a}(\mathbf{D_t}) = \alpha_a ||D(a, b, t)||.$$

Finally, if D(a, b, t) is uniformly distributed, the potential of clique (a) is:

$$V_{C_a}(\mathbf{E_t}, \mathbf{D_t}, \mathbf{f_t}) = V_{C_a}(\mathbf{D_t}) = 0.$$

In this work, we choose the uniform distribution model.

C_b = {Φ(a, b)} - the correlation of the boundary element E(a, b, t) with the intensity edges
 We define the potential of clique (b) to be inversely proportional to the intensity edge factor:

$$V_{C_b}(\mathbf{E_t}, \mathbf{D_t}, \mathbf{f_t}) = V_{C_b}(E(a, b, t), \mathbf{f_t}) = \begin{cases} \frac{E_h(a, b, t)}{\operatorname{edge}_h(a, b, \mathbf{f_t})}, \\ \frac{E_v(a, b, t)}{\operatorname{edge}_v(a, b, \mathbf{f_t})}, \end{cases}$$

where $\operatorname{edge}_h(a, b, \mathbf{f_t})$ and $\operatorname{edge}_v(a, b, \mathbf{f_t})$ measure the degree of discontinuity in the intensity image along the horizontal and vertical directions, respectively. For example, the quantity $\operatorname{edge}_h(a, b, \mathbf{f_t})$ can be defined as the number of significantly large positive or negative transitions between pixels a and b.

• $C_c = \{\Psi(a,b), \Phi_h(a,b), \Psi(a,b-1)\}$ or $\{\Psi(a,b), \Phi_v(a,b), \Psi(a-1,b)\}$ – the correlation between neighbor control vectors.

Note that the boundary element E(a,b,t) between two neighbor control vectors has substantial influence to the correlation of the control vectors. If there is a boundary between the two neighbor control vectors, the two vectors belong to different interpolation object O_i and have no correlation. Otherwise, the two vectors belong to the same object and have strong correlations. We define the potential of clique (c) as

$$V_{C_c}(\mathbf{E_t}, \mathbf{D_t}, \mathbf{f_t}) = V_{C_c}(\mathbf{E_t}, \mathbf{D_t}) = \begin{cases} |D(a, b, t) - D(a, b - 1, t)|, & E_h(a, b, t) = 0, \\ |0, & E_h(a, b, t) = 1. \end{cases}$$

• $\mathbf{C_d} = \{\Phi_h(a,b), \Phi_h(a-1,b), \Phi_v(a,b), \Phi_v(a,b-1)\}$ and $\mathbf{C_e} = \{\Phi_h(a,b), \Phi_v(a,b), \Phi_h(a,b+1), \Phi_v(a+1,b)\}$ – the a prior knowledge of the boundary set $\mathbf{E_t}$.

We define the potential of cliques (d) and (e) according to a prior distribution of the boundary set E_t , i.e.

$$V_{C_d}(\mathbf{E_t}, \mathbf{D_t}, \mathbf{f_t}) = V_{C_d}(\mathbf{E_t}), \quad \text{and} \quad V_{C_e}(\mathbf{E_t}, \mathbf{D_t}, \mathbf{f_t}) = V_{C_e}(\mathbf{E_t}).$$

The consideration in these definitions includes the suppression of boundaries to reduce the number of interpolation regions and the smoothness and closeness of the boundary set E_t to form a reasonable object. The potentials for cliques C_d and C_e are summarized in Figs. 7 and 8.

By using Theorem 1 and the potentials of cliques (a)-(e) defined above, we can obtain a prior distribution of the boundary set E_t and the control vector set D_t as:

$$P(\mathbf{E_t}, \mathbf{D_t} \mid \mathbf{f_t}) = \frac{1}{A_1} \exp\{-U_1(\mathbf{E_t}, \mathbf{D_t}, \mathbf{f_t})\}, \tag{3.4}$$

where A_1 is a normalization factor and

$$U_1(\mathbf{E_t}, \mathbf{D_t}, \mathbf{f_t}) = \sum_{\mathbf{C} \in c(\mathbf{S})} V_C(\mathbf{E_t}, \mathbf{D_t}, \mathbf{f_t})$$

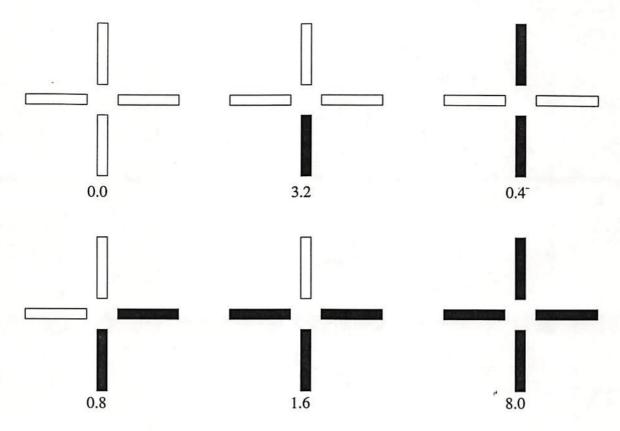


Figure 7: Potential $V_{\mathcal{C}_d}$ (For rotational aliases, only one is listed in the figure)

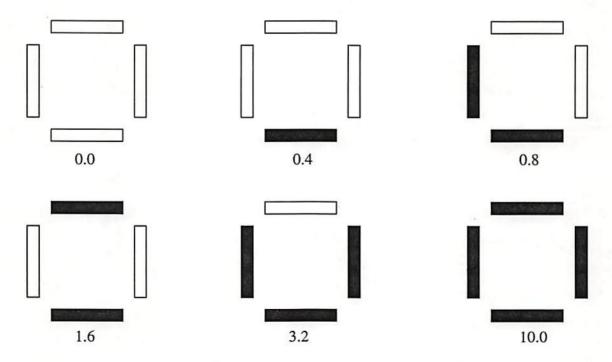


Figure 8: Potential V_{C_e} (For rotational aliases, only one is listed in the figure)

$$= \alpha_b \cdot \sum_{\mathbf{C_b}} V_{C_b}(\mathbf{E_t}, \mathbf{f_t}) + \alpha_c \cdot \sum_{\mathbf{C_c}} V_{C_c}(\mathbf{D_t}, \mathbf{E_t}) + \alpha_d \cdot \sum_{\mathbf{C_d}} V_{C_d}(\mathbf{E_t}) + \alpha_d \cdot \sum_{\mathbf{C_c}} V_{C_e}(\mathbf{E_t}),$$

$$(3.5)$$

and where α_b , α_c , α_d are the weighting factors for different cliques. The value of α_b relates to the degree of correlation between the motion boundary and the intensity edge, the value of α_c relates to the degree of correlation between neighbor control vectors, and the value of α_d relates to a prior restriction of the boundary set E_t . By substituting (3.2), (3.4), (3.5) in (3.1), we obtain

$$P(\mathbf{f_{t-\Delta t}} \mid \mathbf{E_t}, \mathbf{D_t}, \mathbf{f_t}) P(\mathbf{E_t}, \mathbf{D_t} \mid \mathbf{f_t}) = \frac{1}{A} \exp\{-U(\mathbf{E_t}, \mathbf{D_t}, \mathbf{f_t}, \mathbf{f_{t-\Delta t}})\},$$
(3.6)

where A is a normalization factor and

$$U(\mathbf{E_{t}}, \mathbf{D_{t}}, \mathbf{f_{t}}, \mathbf{f_{t-\Delta t}}) = \frac{1}{2\sigma^{2}} \sum_{(x,y)\in\mathbf{I}} DFD^{2}(x, y, t) + \alpha_{b} \cdot \sum_{\mathbf{C_{b}}} V_{C_{b}}(\mathbf{E_{t}}, \mathbf{f_{t}})$$

$$+ \alpha_{c} \cdot \sum_{\mathbf{C_{c}}} V_{C_{c}}(\mathbf{E_{t}}, \mathbf{D_{t}}) + \alpha_{d} \cdot [\sum_{\mathbf{C_{d}}} V_{C_{d}}(\mathbf{E_{t}}) + \sum_{\mathbf{C_{e}}} V_{C_{e}}(\mathbf{E_{t}})]. \quad (3.7)$$

The four terms in (3.7) are called, respectively, the displacement frame difference, the correlation between the motion boundary (motion discontinuity) and the intensity edges, the correlation between neighbor control vectors, and the *a prior* restriction of the boundary set $\mathbf{E_t}$.

3.3 Estimation via Optimization

By using the analysis given above, the problem of finding the MAP estimation of the motion field $d^*(x, y, t) = gen\{\mathbf{E}_{\mathbf{t}}^*, \mathbf{D}_{\mathbf{t}}^*\}$ is converted to the determination of the minimum point of the potential $U(\mathbf{E}_{\mathbf{t}}, \mathbf{D}_{\mathbf{t}}, \mathbf{f}_{\mathbf{t}}, \mathbf{f}_{\mathbf{t}-\Delta \mathbf{t}})$, i.e.

$$U(\mathbf{E}_{t}^{*}, \mathbf{D}_{t}^{*}, \mathbf{f}_{t}, \mathbf{f}_{t-\Delta t}) = \min_{\mathbf{E}_{t} \in \mathcal{E}_{t}, \mathbf{D}_{t} \in \mathcal{D}_{t}} U(\mathbf{E}_{t}, \mathbf{D}_{t}, \mathbf{f}_{t}, \mathbf{f}_{t-\Delta t}),$$
(3.8)

where the potential $U(\mathbf{E_t}, \mathbf{D_t}, \mathbf{f_t}, \mathbf{f_{t-\Delta t}})$ is given by (3.7). To obtain the global minimum of the potential function $U(\mathbf{E_t}, \mathbf{D_t}, \mathbf{f_t}, \mathbf{f_{t-\Delta t}})$ is not an easy task. On one hand, since the configuration space $\{\mathcal{E}_t, \mathcal{D}_t\}$ of the BCV motion field is extremely large, it is impractical that we search the whole space for the minimum point. On the other hand, since the potential $U(\mathbf{E_t}, \mathbf{D_t}, \mathbf{f_t}, \mathbf{f_{t-\Delta t}})$ is a highly nonconvex function with many local extrema and the boundary element E(d, a, b, t) takes a binary value, we cannot adopt a gradient based algorithm to find the minimum point. Since the problem formulation involves the MRF, a standard simulated annealing [9] process is used to solve this problem. We update the control vector D(a, b, t) and the boundary element E(a, b, t) once at

a time, and a decreasing temperature sequence T_k is used to control the update along the process. For each update, the change in the potential U is evaluated together with the temperature T_k to determine whether the update is accepted or not. In the beginning, the temperature T_k is high so that the update is very random to allow the algorithm to select a good starting point to avoid being trapped into a local minimum. As time proceeds, the temperature T_k is decreasing and the update tends to accept lower potential and the system is gradually running towards the global minimum. The original simulated annealing is very slow. In this paper, several novel techniques are used to accelerate the annealing procedure. They include the selection of a good initial motion field by using a multiresolution tree (MRT) based algorithm [13], the logarithmic rate temperature reduction, the stochastic relaxation of the control vector set $\mathbf{D_t}$ and a fast control vector search, etc. We refer to [12] for more details. By using all the acceleration techniques, we can get a BCV motion estimation algorithm which requires about twice of the computational cost of the exhaustive block search.

4 Coding of Displacement Frame Difference

As discussed in Section 2, the BCV-based displacement frame difference (DFD) is different from that of the conventional block based scheme. Inside each object, there is no block effect and the main distortion is geometrical deformation which is less sensitive subjectively. Around the boundaries of an object, the distortion is similar to that of the block based scheme. It is desirable to find a distortion measure that helps to select the DFD for encoding to enhance the overall performance of the encoder. We develop a criterion called the pixel threshold (PT) criterion which evaluates the DFD of each block by two factors: the position factor p(a, b) and the error factor e(a, b).

When the block is located at an object boundary, its position factor p(a, b) takes value one; otherwise, it is zero. Thus, p(a, b) = 1 (or 0) means that block B(a, b) is a boundary (or internal) block. The value e(a, b) is the sum of the absolute value of DFD above a certain threshold Q within a given block. Mathematically, it can written as

$$e(a,b) = \sum_{(x,y)\in B(a,b)} \left\lfloor \frac{|DFD(x,y,t)|}{Q} \right\rfloor,\tag{4.9}$$

where Q is a threshold and $\lfloor x \rfloor$ means the largest integer value that is not greater than x. The PT decision is:

$$\begin{cases} p(a,b) = 0 \text{ and } e(a,b) > T_0 & \text{to be encoded} \\ p(a,b) = 1 \text{ and } e(a,b) > T_1 & \text{to be encoded} \\ \text{other cases} & \text{not to be encoded} \end{cases}$$

$$(4.10)$$

Note that in above T_0 and T_1 denote two different thresholds for internal and boundary blocks, respectively. It is often to choose $T_0 \gg T_1$, since the distortion of the internal block in the BCV scheme is mainly geometrical deformation which allows a larger value of error tolerance.

5 Experimental Results

Experiments are performed to compare the BCV scheme with the traditional block-based method used in the MPEG standard. The test video data include CLAIRE, MISSA, TREVOR, SALES sequences. All of them are of the CIF format with a spatial resolution of 352×288 pixels and a frame rate of 10 frames per second. We apply the exhaustive search scheme to determine the motion vector for each block in the block-based method. For the proposed BCV scheme, each boundary element is encoded by one bit while the control vectors and the displacement frame differences (DFD) are encoded by using the MPEG-I bit stream. We split the DFD into macroblock and encode them according to the pixel threshold criterion as detailed in Section 4. It is worthwhile to point out that although the bit stream of BCV video encoder is similar to that of the MPEG standard, they are essentially different in the motion field representation. Due to the incorporation of the boundary element, the BCV video coder/decoder is not compatible with the MPEG standard. However, it can be implemented by slightly modifying the MPEG code.

We show in Table 1 the average number of bits required to encode the motion field. Since the motion field in the BCV scheme consists of two components — the set $\mathbf{E_t}$ of boundary element functions and the set $\mathbf{D_t}$ of control vectors, we list the individual rate in the third and fourth rows in Table 1. The predictive gain listed in Table 1 is calculated as the average of the following instantaneous gain

Gain(t) =
$$10 \log \frac{255^2}{\sum DFD^2(x, y, t)}$$
,

where the summation is over all pixels. We see from Table 1, the predictive gain of the BCV motion field is higher than the traditional full block matching method from 0.5 to 1.8 dB. This demonstrates that the BCV motion representation is superior to the block-based representation.

Experiments have also been performed to compare the BCV-based video coding scheme with the MPEG-I algorithm [6]. The results are shown in Table 2, where the rate is the average number of coding bits per pixel and the peak signal-to-noise ratio (PSNR) is calculated as the average of the instantaneous PSNR:

$$PSNR(t) = 10 \log \frac{255^2}{\sum \left[f(x, y, t) - \hat{f}(x, y, t) \right]^2},$$
 (5.1)

Item	CLAIRE	MISSA	SALES	TREVOR
Rate in bpp (full block match)	0.0075	0.0108	0.0136	0.0186
Rate in bpp (BCV)	0.0135	0.0185	0.0172	0.0228
Rate in bpp (BCV - E _t)	0.0074	0.0074	0.0074	0.0074
Rate in bpp (BCV – $\mathbf{D_t}$)	0.0061	0.0111	0.0098	0.0154
Gain in dB (full block match)	34.46	33.83	28.11	29:80
Gain in dB (BCV)	35.68	34.37	28.57	31.57

Table 1: Bit rates and gains for the coding of the motion field.

Item	CLAIRE	MISSA	SALES	TREVOR
Rate in bpp (MPEG-I)	0.0237	0.0251	0.0886	0.0819
PSNR in dB (MPEG-I)	35.31	34.49	28.77	31.04
Rate in bpp (BCP)	0.0152	0.0209	0.0750	0.0550
PSNR in dB (BCP)	35.81	34.62	28.86	31.77

Table 2: Bit rates and PSNR values for video sequence coding.

where the summation is over all pixels in an image. One can clearly see from Table 2 that, compared with MPEG-I, BCV video coding achieves a saving of 15-35% in the bit rate with nearly the same PSNR value. To further compare the performance of the MPEG-I and BCV, we plot the bit rate and the PSNR value as a function of the frame number for the CLAIRE and TREVOR test video sequences in Figs. 9 and 10, respectively.

Compared with the MPEG-I coded video, the BCV coded sequence appears to be smoother and clearer with less noisy patterns.

6 Conclusion and Extension

A new motion field representation and estimation framework based on the boundary-control vector (BCV) scheme and the Markov random field model was presented. The BCV motion field is generally continuous with discontinuity only at the object boundaries. It was demonstrated to be a promising method for video coding for the good rate-distortion performance. At present, the major disadvantage of the BCV scheme is its high computational complexity for motion filed estimation. We feel that the computational cost can be reduced by using a multiresolution approach, and a multiresolution BCV motion representation and estimation scheme is under our current study.

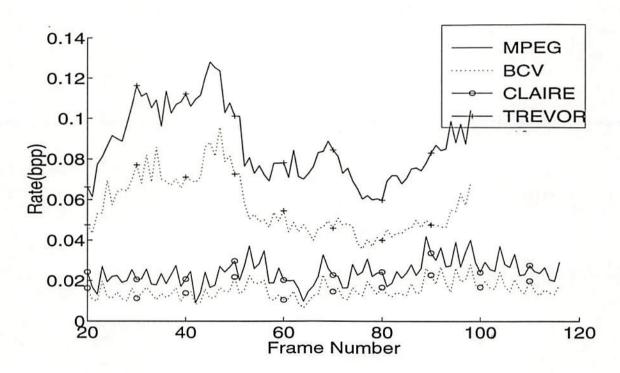


Figure 9: Comparison of coding rate between BCV scheme and MPEG-I scheme

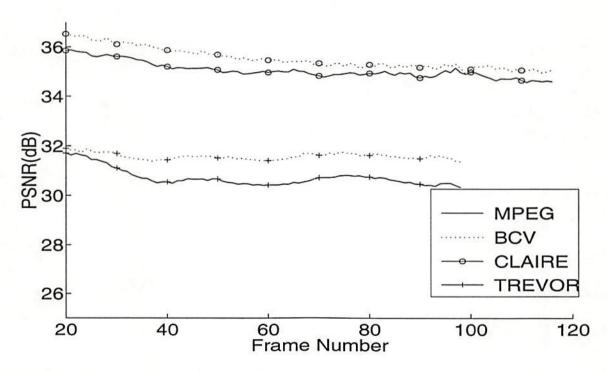


Figure 10: Comparison of coding PSNR between BCV scheme and MPEG-I scheme

Another interesting topic is to further improve the quality of the coded video images. We observe that even though the block effect in the DFD can be greatly reduced by using the BCV scheme, the subsequent DCT-based coding of the DFD still introduces the block effect. A better performance may be achieved by using a wavelet approach to encode the DFD.

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