

**Optimization techniques for adaptive  
quantization of image and video under delay  
constraints**

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## ABSTRACT

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Traditionally, rate-distortion (R-D) theory has been concerned with providing bounds on the optimal performance for various classes of coding algorithms and sources. In this thesis we depart from that approach in two ways. First, our objective are operational R-D results, i.e. we study algorithms that can find the optimal solution for a given coder configuration and known inputs, without relying on modeling either the encoder or the source. Second, we seek to explore explicitly other parameters that determine the achievable R-D performance, namely, the encoding delay and complexity, and the memory at the encoder.

We compute the optimal solution even if it requires too much complexity, memory or delay to be considered in a practical setting. Optimal schemes serve as a benchmark and can also be the basis for heuristic methods which provide slightly suboptimal but more efficient performance. More specifically we study the following topics:

(i) Optimal buffer constrained quantization. We find optimal solutions for the buffer control problem in a deterministic framework by assuming a long encoding delay. Our solution, based on dynamic programming, also leads us to short delay, lower complexity heuristics.

(ii) Rate control and policing constraints for video transmission over ATM networks. We study the problem of optimizing the source quality as in (i), while taking into account network considerations.

(iii) Optimization of dependent quantization environments. Optimal bit alloca-

tion results are presented for dependent quantization schemes (e.g. DPCM, predictive motion compensated video coding, MPEG).

(iv) Rate-delay trade-offs in a multiresolution image database system. We study how the bit allocation in a multiresolution coding system can be chosen so as to minimize the end-to-end query delay in browsing through a set of images.

(v) Adaptive quantization without side information. We propose a backward adaptive quantization algorithm where the input distribution is “learned” from past quantized samples. This allows adaptation to sources with unknown or time-varying input distribution.

## List of Abbreviations

ATM	–	Asynchronous Transfer Mode
B	–	Bidirectionally interpolated mode (in MPEG)
CBR	–	Constant Bit Rate
DCT	–	Discrete Cosine Transform
DP	–	Dynamic Programming
DPCM	–	Differential Pulse Coded Modulation
GAP	–	Generalized Assignment Problem
HDTV	–	High Definition Television
HVS	–	Human Visual System
I	–	Intraframe mode (in MPEG)
JPEG	–	Joint Photographic Experts Group
KLT	–	Karhunen Loève Transform
LB	–	Leaky Bucket
MPEG	–	Moving Pictures Experts Group
MR	–	Multiresolution
MSE	–	Mean Squared Error
P	–	Prediction mode (in MPEG)
PSNR	–	Peak Signal to Noise Ratio
R-D	–	Rate–Distortion
SBC	–	Subband Coding
SMG	–	Statistical Multiplexing Gain

SNR – Signal to Noise Ratio  
SR – Single resolution  
TCM – Trellis Coded Modulation  
TCQ – Trellis Coded Quantization  
VBR – Variable Bit Rate  
VA – Viterbi Algorithm  
VLSI – Very Large Scale Integration  
VQ – Vector Quantization

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A mis padres